

Algebra 1

Factoring Special Products



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Difference of Squares



Perfect Square

Factor by Grouping

Guidelines for Factoring Polynomials Completely

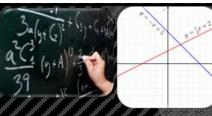
Overview 

$(a + b)(a - b) =$

$$a^2 - b^2 = (a + b)(a - b)$$

$4x^2 - 25 = (2x + 5)(2x - 5)$

$(2x)^2 - 5^2$



Difference of Two Squares 

Find the factors or $8 - 18x^2$

You Try

$8 - 18x^2 = 2(4 - 9x^2)$

$= 2(2 + 3x)(2 - 3x)$

Find the factors or $8 - 18x^2$

You Try

$$(a + b)^2 = (a + b)(a + b)$$

$$a^2 + ab + ab + b^2$$

$$= a^2 + 2ab + b^2$$

$$(a - b)^2 = (a - b)(a - b)$$

$$a^2 - ab - ab + b^2$$

$$= a^2 - 2ab + b^2$$

Perfect Squares

$$\begin{aligned} & x^3 + 3x^2 + 5x + 15 \\ &= x^2(x + 3) + 5(x + 3) \\ &= (x + 3)(x^2 + 5) \end{aligned}$$

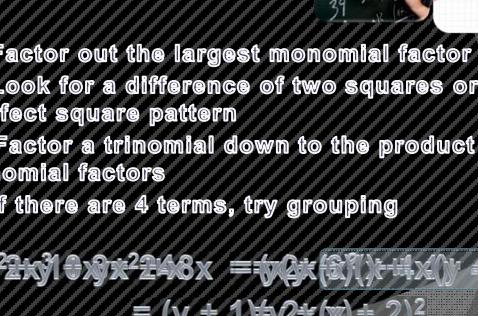


A dark, star-filled background image of space, featuring several bright stars and a few faint, glowing nebulae or galaxies.



$$\begin{aligned} & x^3 + 13x^2 - 5x - 65 \\ & x^2(x + 13) - 5(x + 13) \\ & (x + 13)(x^2 - 5) \\ \text{factor: } & x^3 - 5x + 13x^2 - 65 \end{aligned}$$





1. Factor out the largest monomial factor

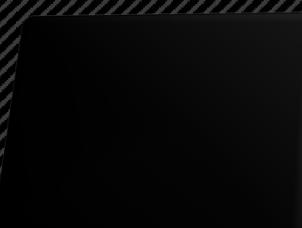
2. Look for a difference of two squares or a perfect square pattern

3. Factor a trinomial down to the product of binomial factors

4. If there are 4 terms, try grouping

$$\begin{aligned} y^{22} + xy^{10}y^8x^2 + 48x &= y^2(x^{11}(y^4) + x(y^4)(1)) \\ &= (y + 1)x^2(x + 2)^2 \end{aligned}$$

ctor completely:

$$z^4 + 24z^3 + 48z^2$$


You Try It

Factor completely:

$$z^4 + 24z^3 + 48z^2$$

$$= 3z^2(z^2 + 8z + 16)$$

$$= 3z^2(z + 4)^2$$

factor completely:

$$m^3 + 4m^2 - 25m - 100$$




You Try 

factor completely:

$$(m^3 + 4m^2) - (25m + 100)$$




You Try 

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